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## How to Read the ESR Curve of Capacitors

Istvan Novak

# Outline

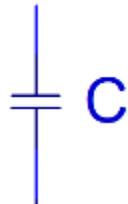
- What is ESR, why should we care
- The impedance of capacitors
- Frequency dependency of ESR
- Sources of ESR
- Getting the series equivalent circuit
- Measured examples
- ESR: what is guaranteed by spec
- How much ESR varies
- Consequences of ESR variations
- Secondary effects
- Summary

# Effective Series Resistance (ESR)

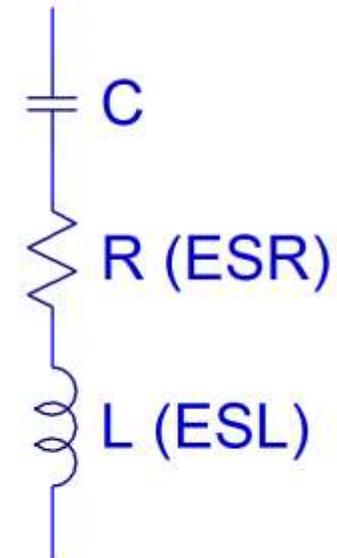
Why should we care for ESR?

- RF/MW: dissipative losses, unloaded Q of circuit
- PI: PDN impedance, ripple dissipation
- SI: loss in DC blocking applications

Ideal capacitor  
No parasitics

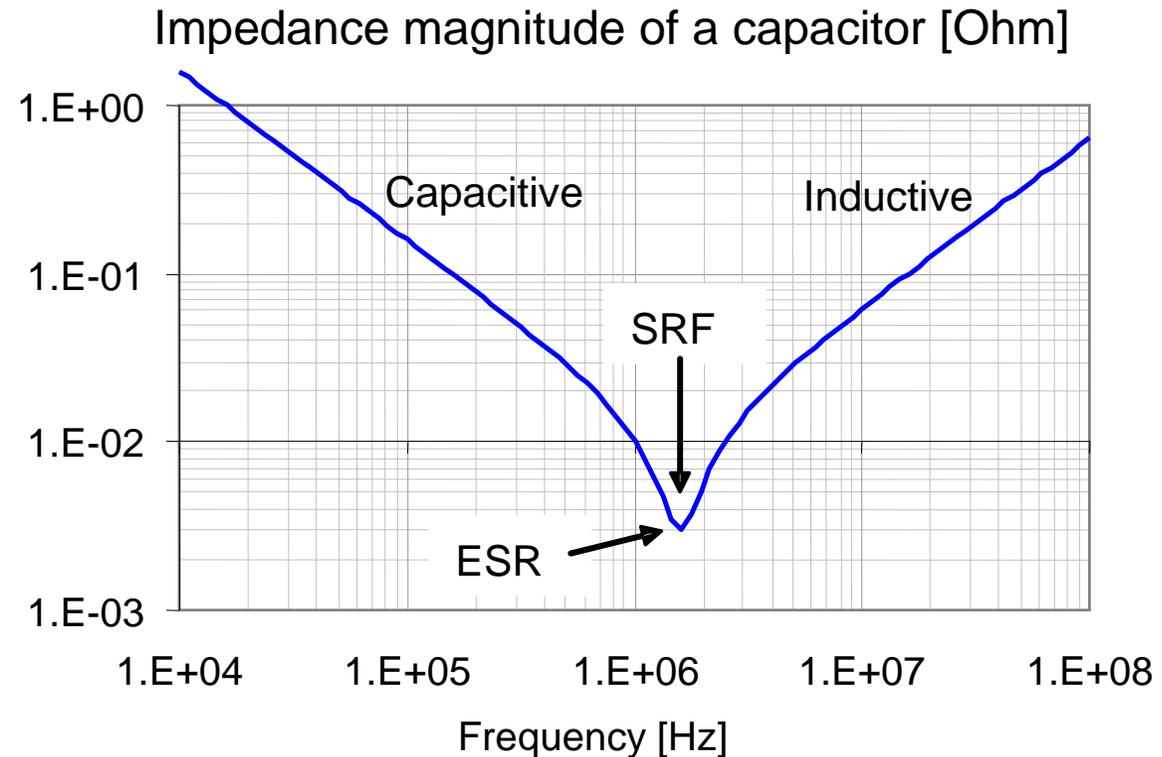
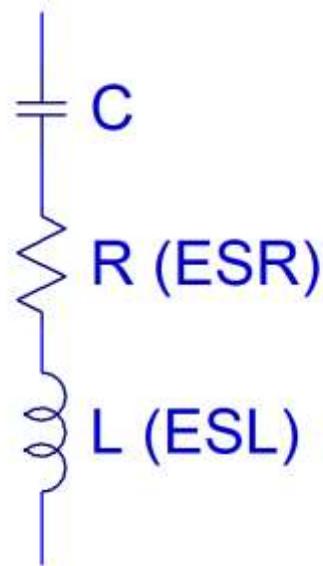


Real capacitor  
ESR and ESL parasitics



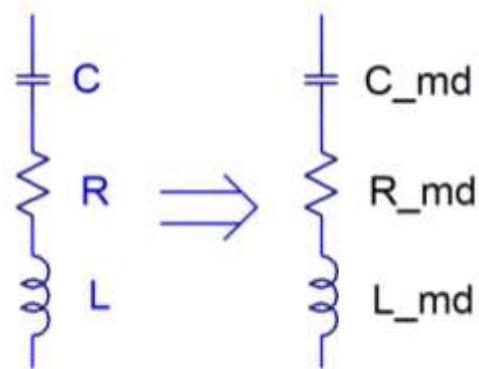
# The Impedance of Capacitors

A simple equivalent circuit of a capacitor including its resistance and inductance

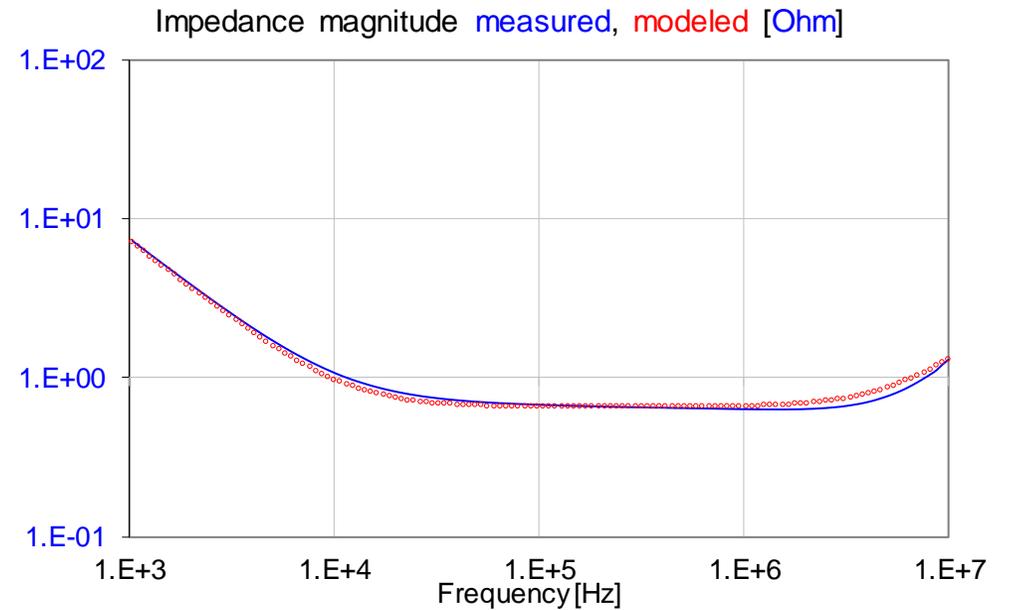


# How Accurate Is the C-R-L Model?

A simple equivalent circuit of a 22uF electrolytic capacitor with frequency-independent resistance and inductance

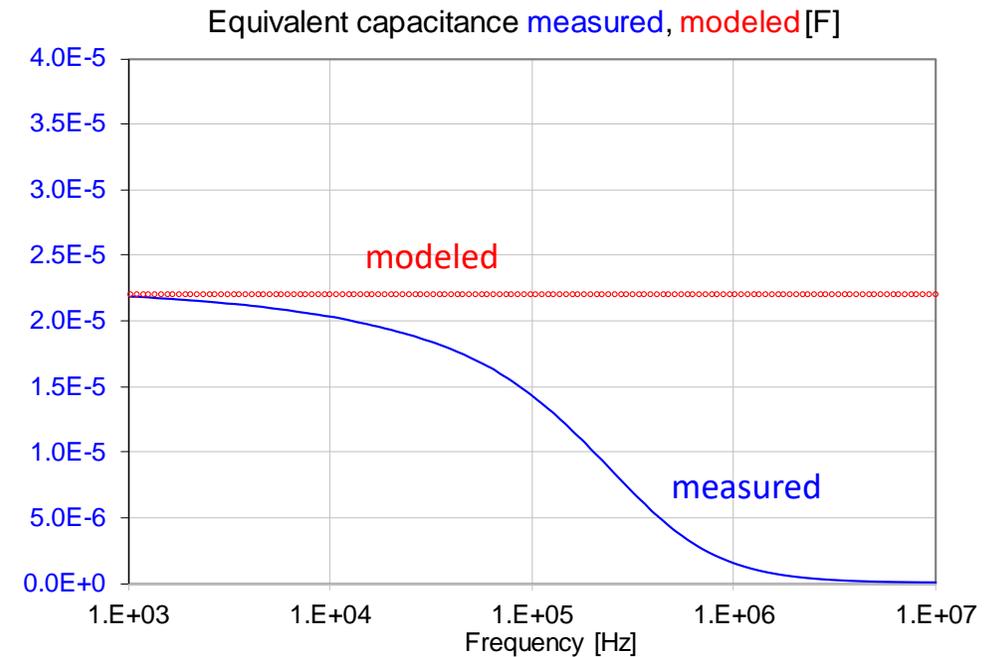
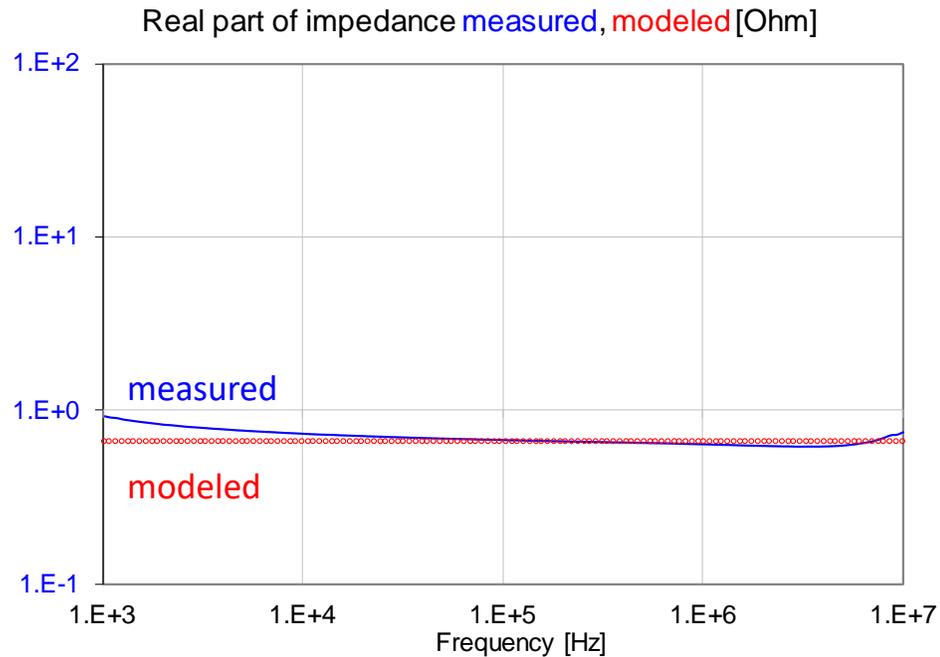


MODEL PARAMETERS:  
C\_md R\_md L\_md  
2.20E-05 6.50E-01 1.80E-08



# How Accurate Is the C-R-L Model?

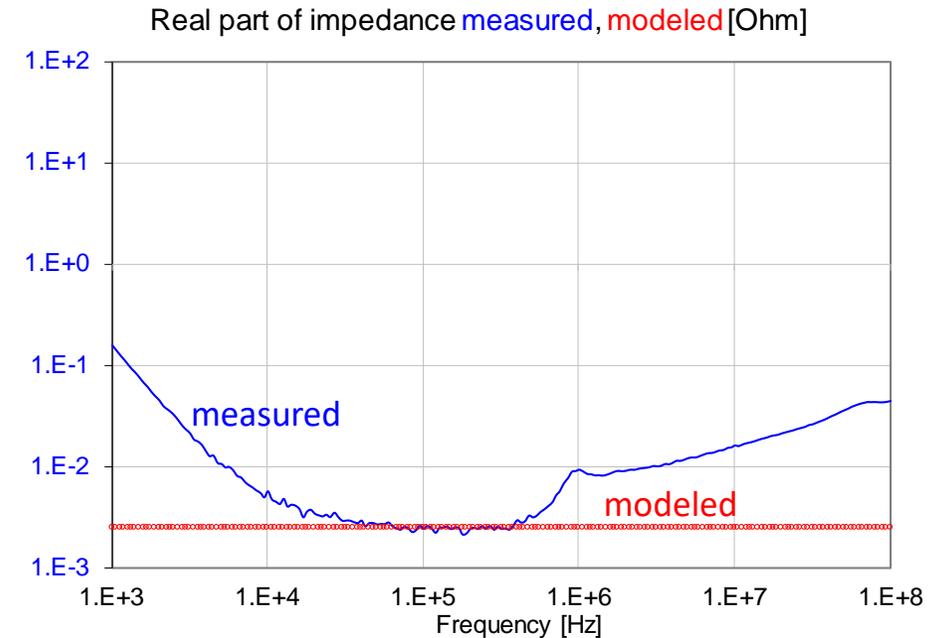
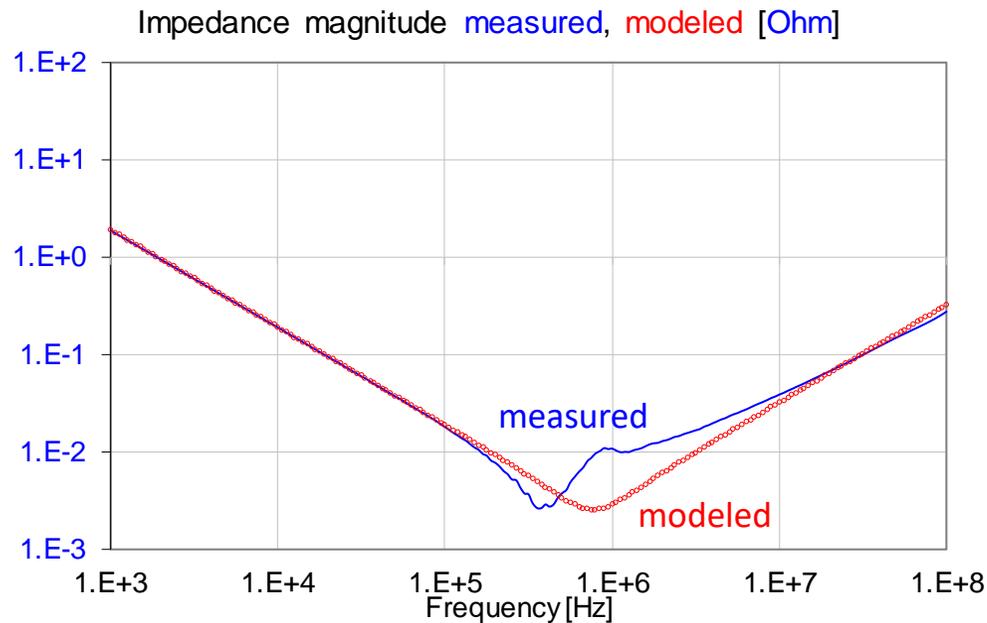
The frequency-independent ESR is fairly accurate (for this part, in this frequency range)



# How Accurate Is the C-R-L Model?

The frequency-independent ESR is a fairly bad fit for a 100uF MLCC part

MODEL PARAMETERS:  
 C\_md R\_md L\_md  
 8.50E-05 2.50E-03 5.00E-10

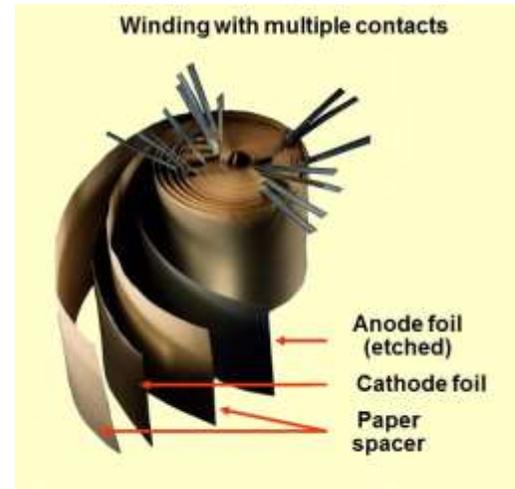


# Effective Series Resistance: Its Sources

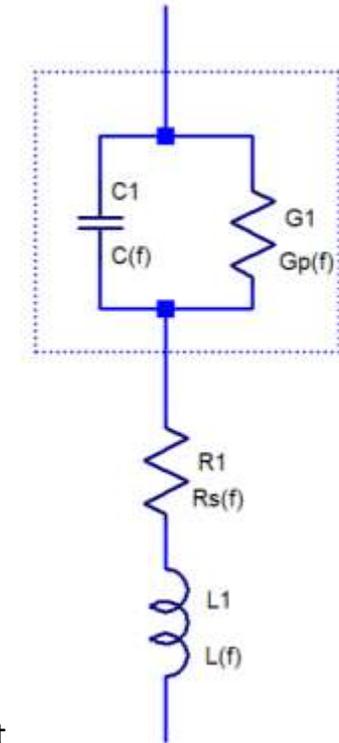
- Conductor loss ( $R1$ ): terminals, capacitor plates
- Dielectric loss ( $G1$ ): dielectric loss tangent of insulating material, surface leakage



Source  
<https://go.kemet.com/en-us/en-us/06-2020-webinar-mlcc-and-film-construction-characteristics>



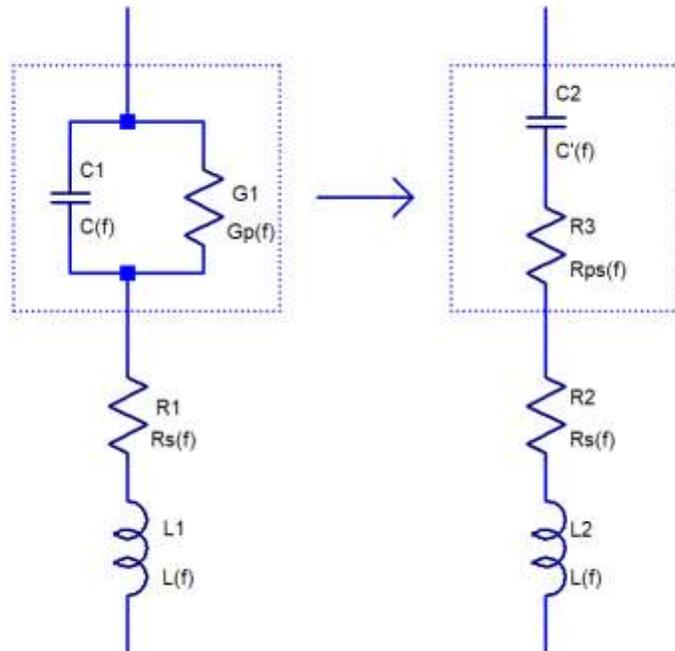
Source  
[https://en.wikipedia.org/wiki/Aluminum\\_electrolytic\\_capacitor#/media/File:Al-e-cap-winding-multi-tabs.jpg](https://en.wikipedia.org/wiki/Aluminum_electrolytic_capacitor#/media/File:Al-e-cap-winding-multi-tabs.jpg)



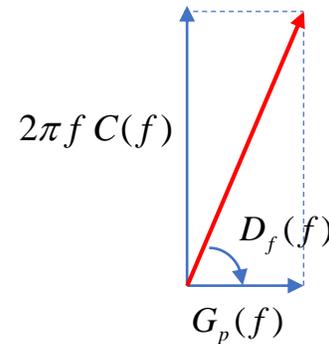
# What Makes ESR Frequency Dependent?

Multiple reasons:

- G1 is frequency dependent
  - For a given  $D_f(f)$  dielectric loss tangent G1 is
- R1 is frequency dependent due to current redistribution
- G1 and R1 are mixed through opposite-sign reactance



Admittance of capacitors

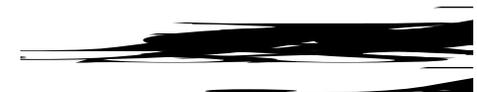


Frequency dependence of capacitance and dielectric loss

$$C(f) = C(f_0) \left( 1 - D_f(f_0) \text{Ln} \left( \frac{f}{f_0} \right) \frac{1}{\pi/2} \right)$$



Frequency dependence of conductive loss due to skin effect



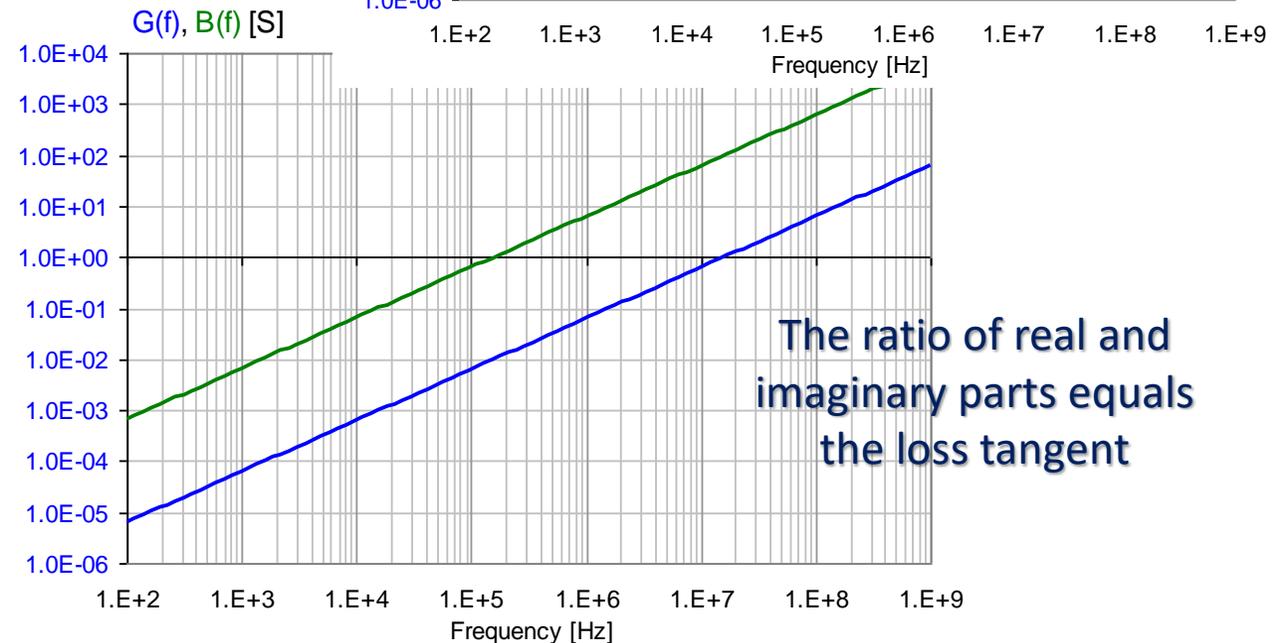
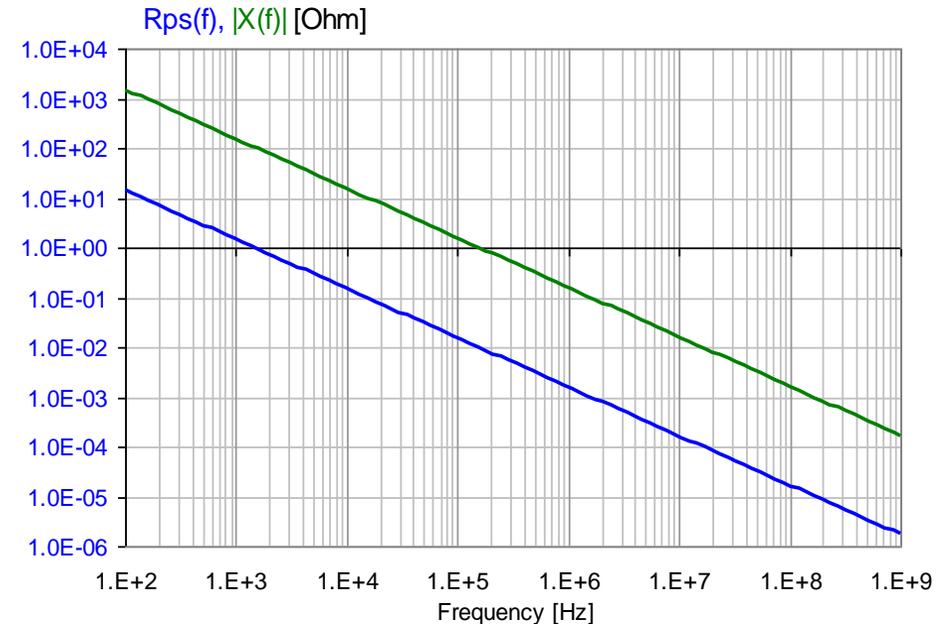
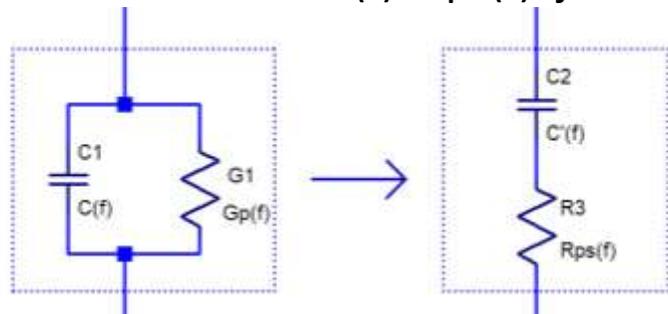
# The Combination of Series and Parallel Losses

The conversion:

- Step 1: Convert the parallel R-C to a series R-C network
- Step 2: Add the series R-L network related to conductive losses
- Converting parallel to serial circuit mixes the real and imaginary parts

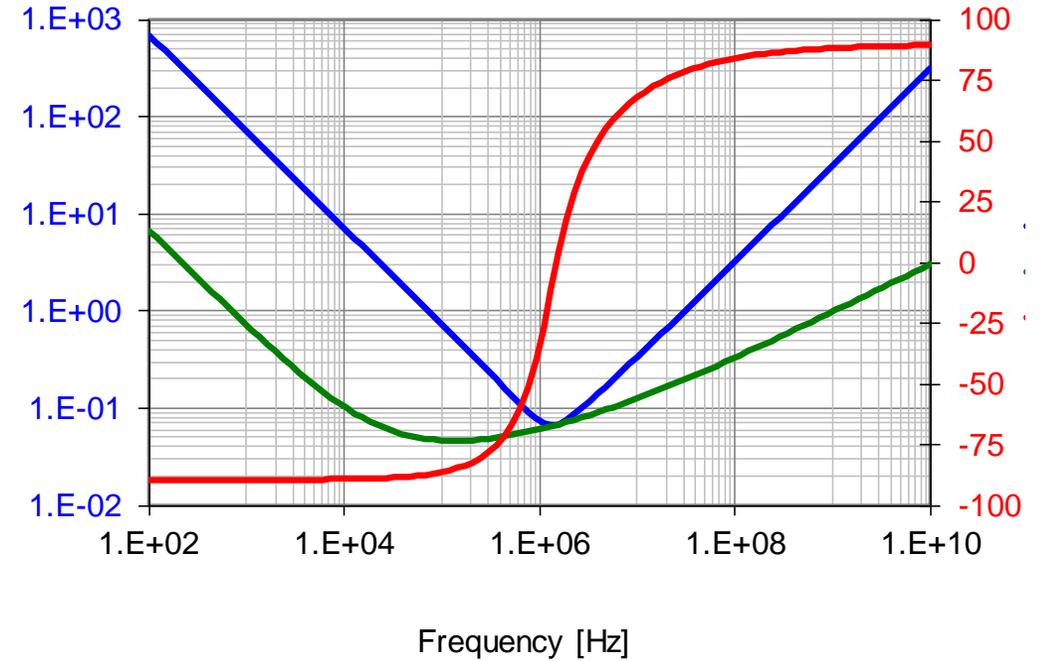
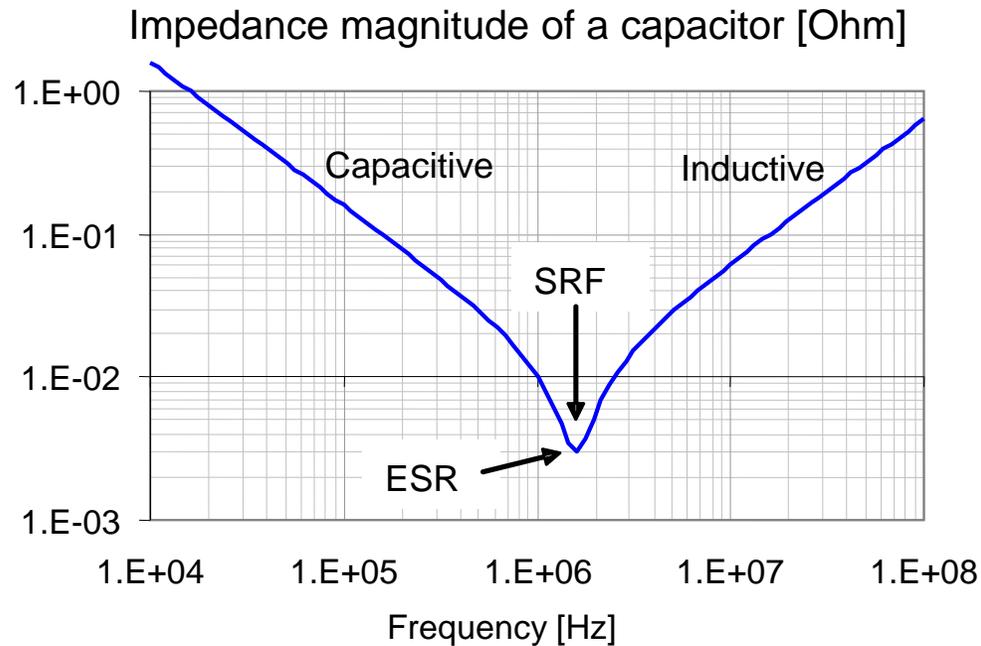
$$Y_p(f) = G_p(f) + j2\pi f C(f)$$

$$Z_s(f) = R_{ps}(f) + j2\pi f C(f)$$

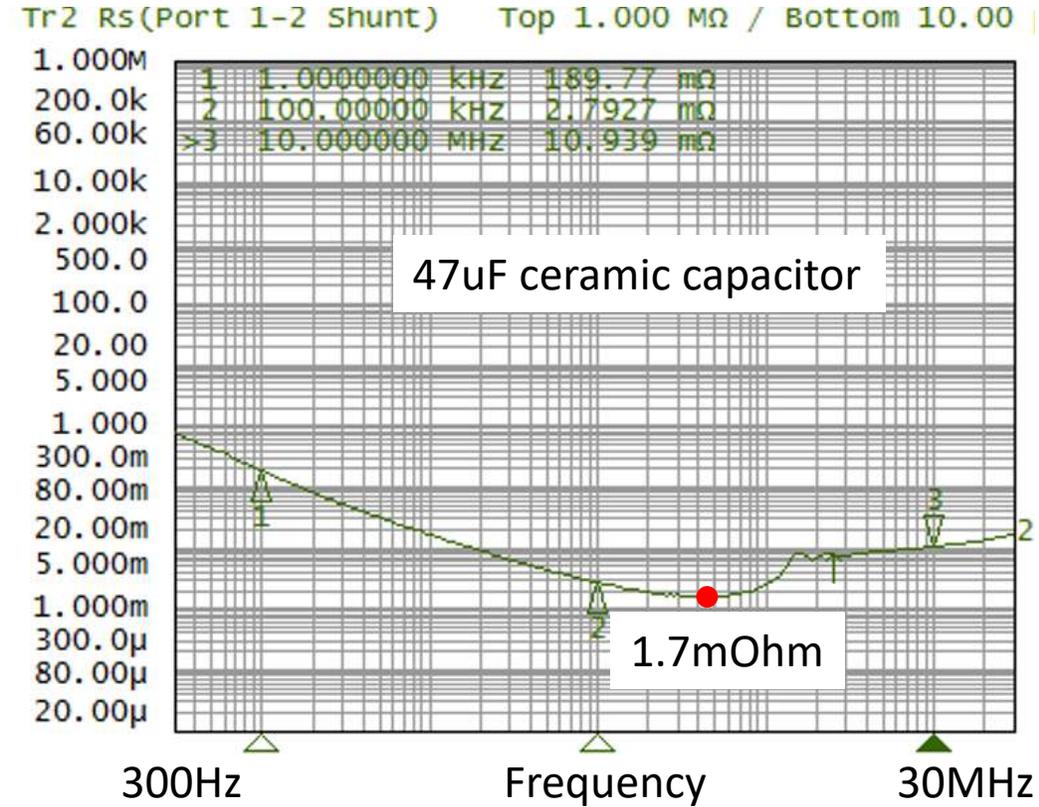
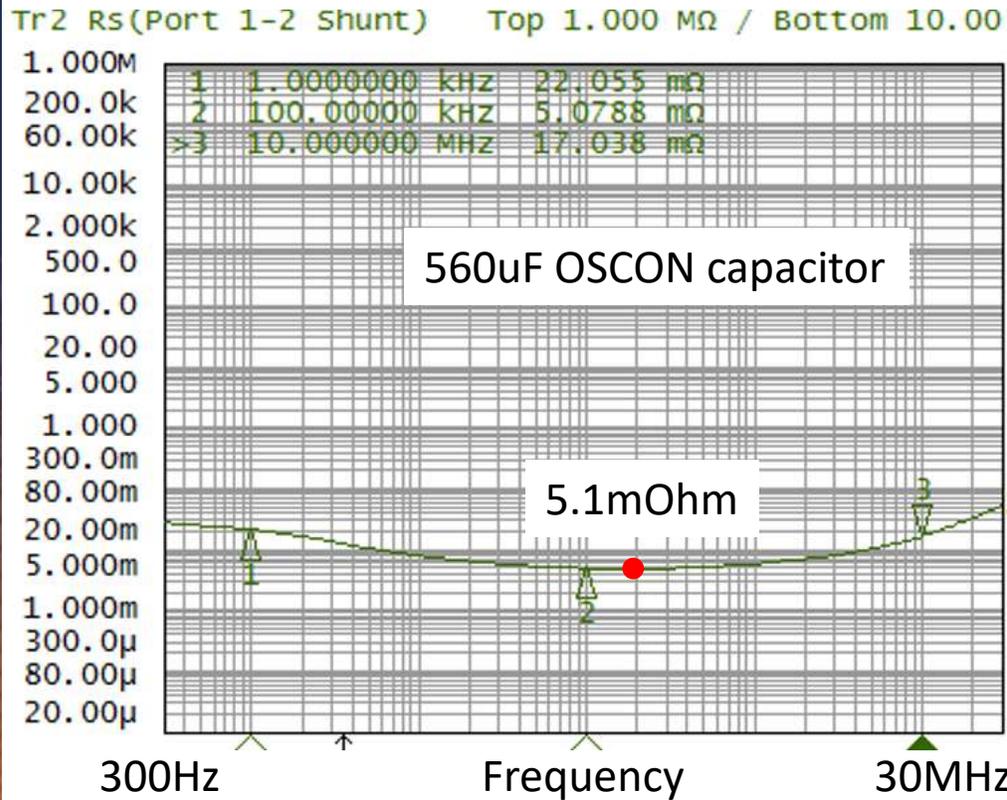
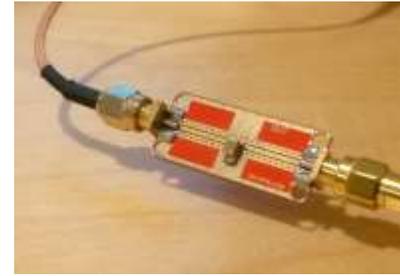
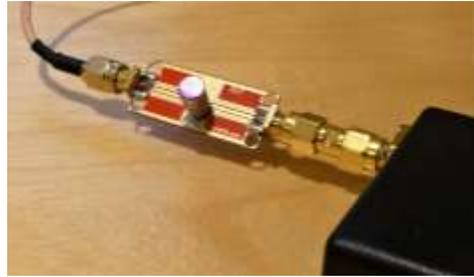


# The Combined Series and Parallel Losses

Impedance magnitude, real part and phase of capacitor  
[Ohm, Ohm, deg]



# Some Measured ESR Examples

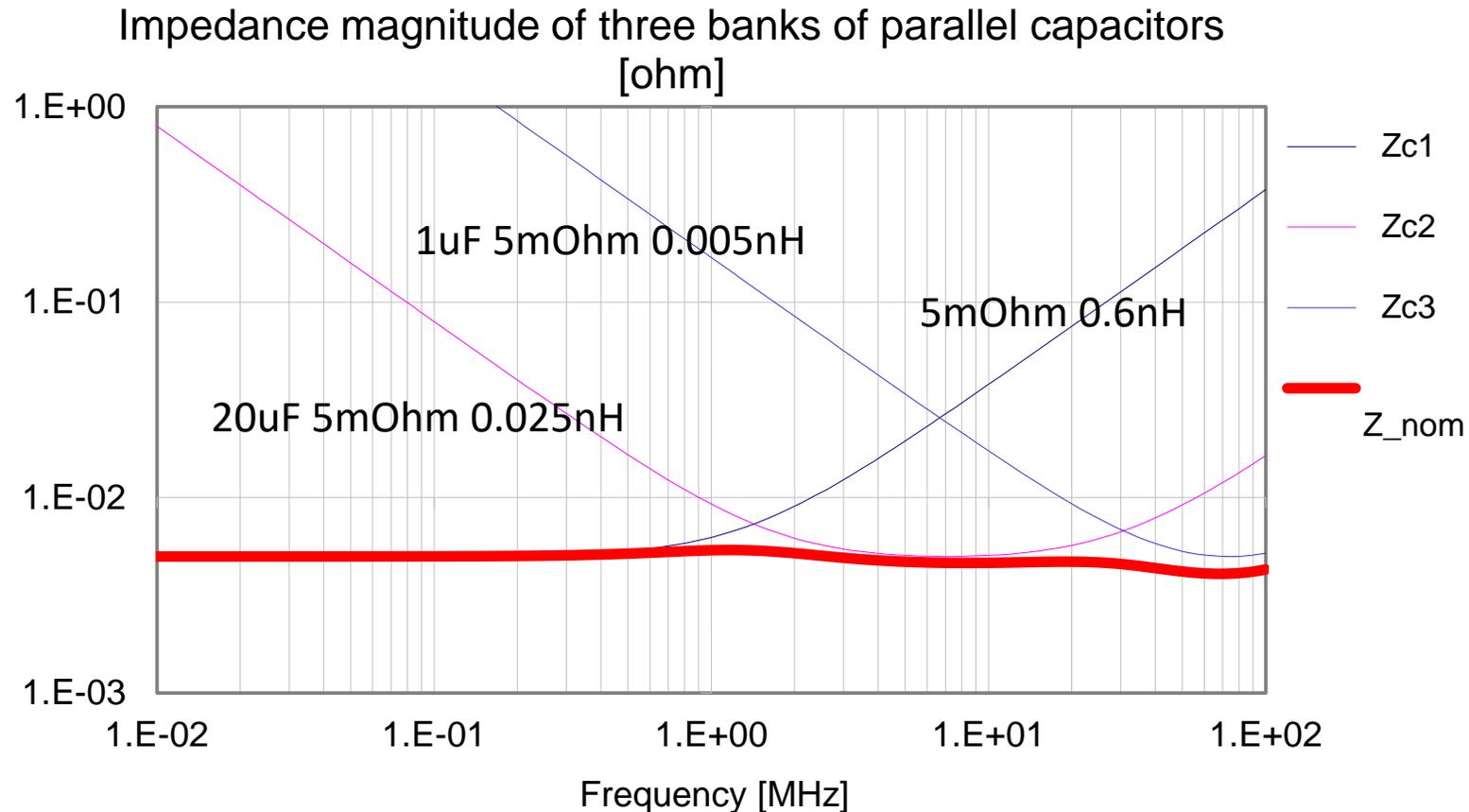


# ESR: What is Guaranteed by Spec?

- MLCC: we get typical ESR values at best
- Tantalum, electrolytic capacitors: at best we get the maximum ESR values
- Exception: controlled-ESR capacitors
- Don't forget some additional conditions: aging, thermal shock, etc

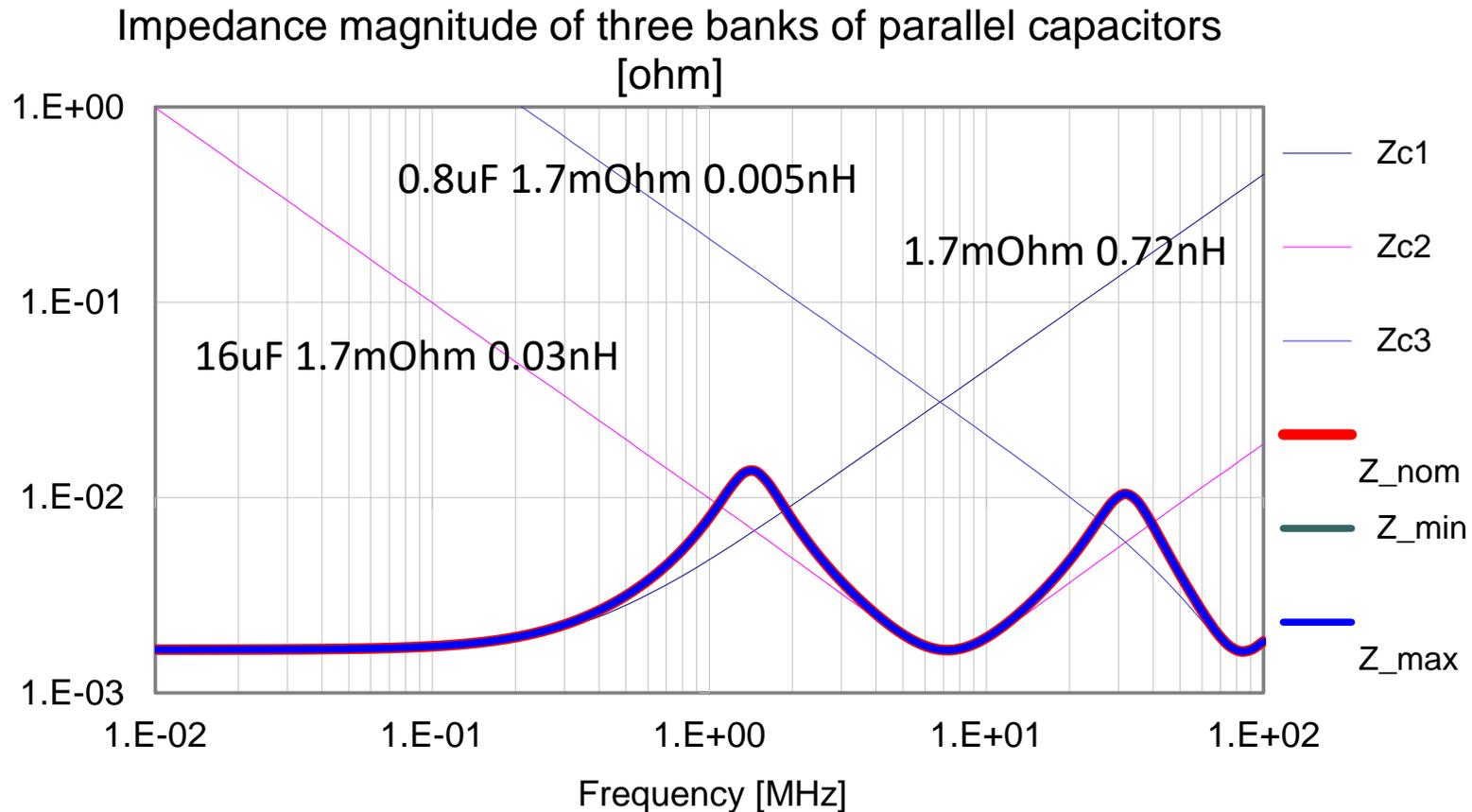
# ESR Uncertainty: Why Should We Care?

An example with three banks of PDN parts, nominally producing flat 5mOhm lumped impedance



# ESR Uncertainty: Worst Case

Assume 1/3x...3x ESR variation and +/-20% C and L variations



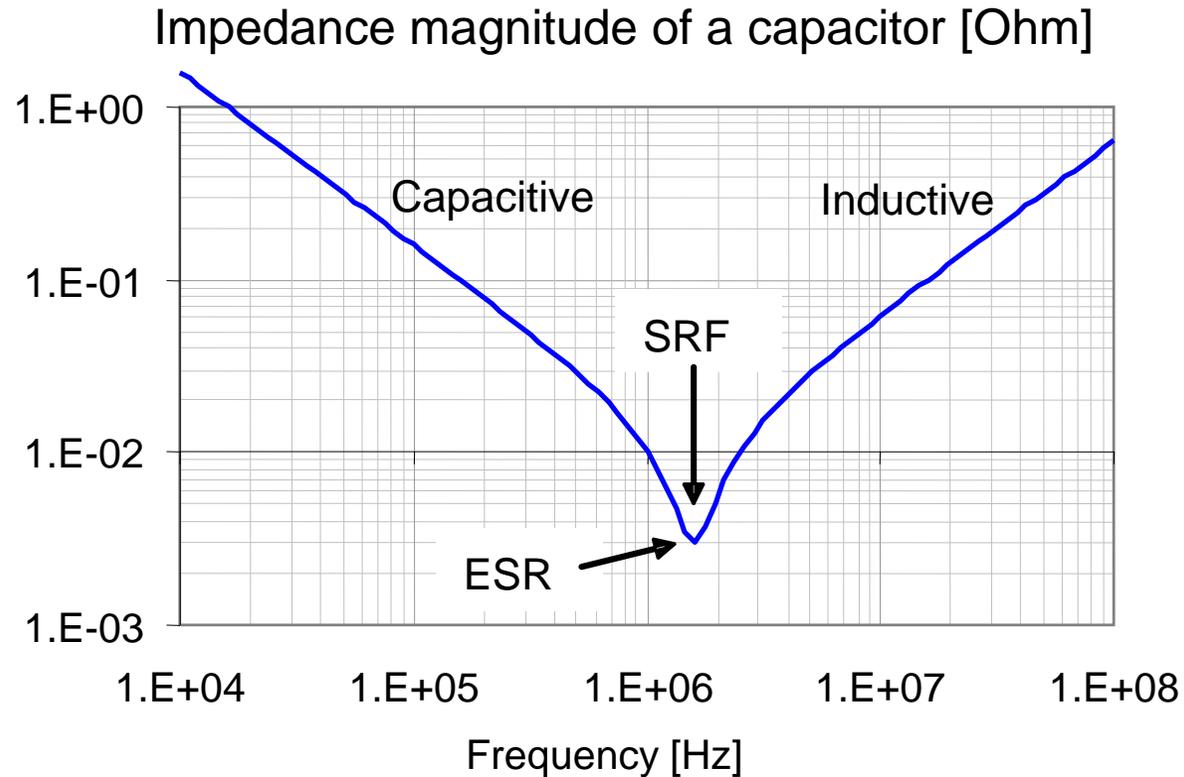
**WC transient  
noise: 19  
mVpp/A**

# What Frequency Range Should We Care?

Usually, the vicinity of SRF matters

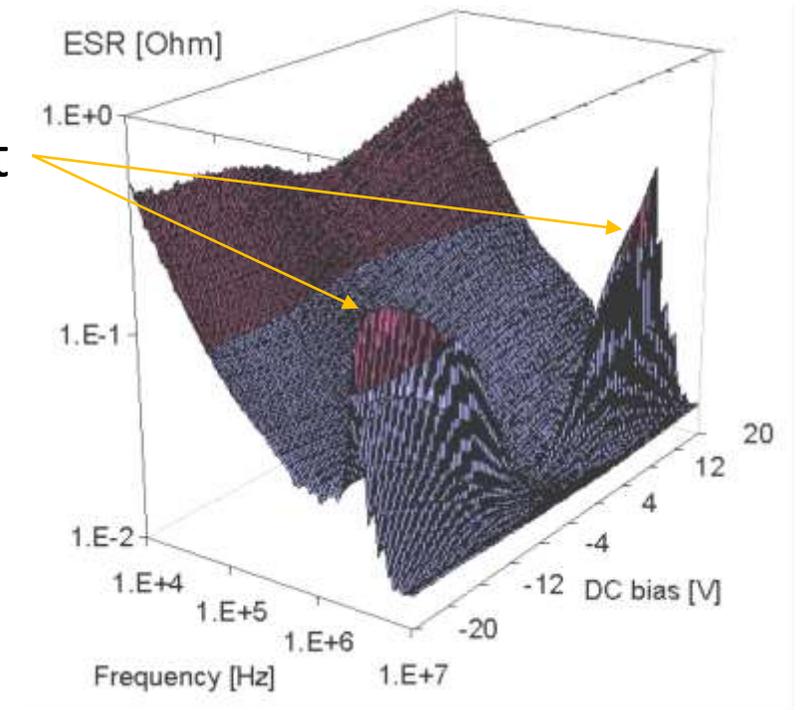
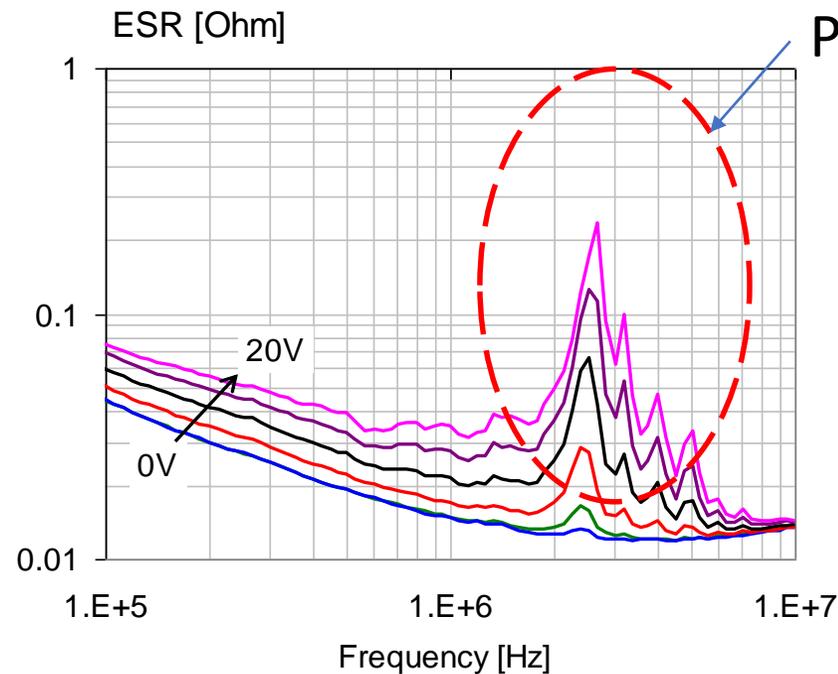
At much lower and higher frequencies other PDN components will dominate

Note: some simulators may use truncated values



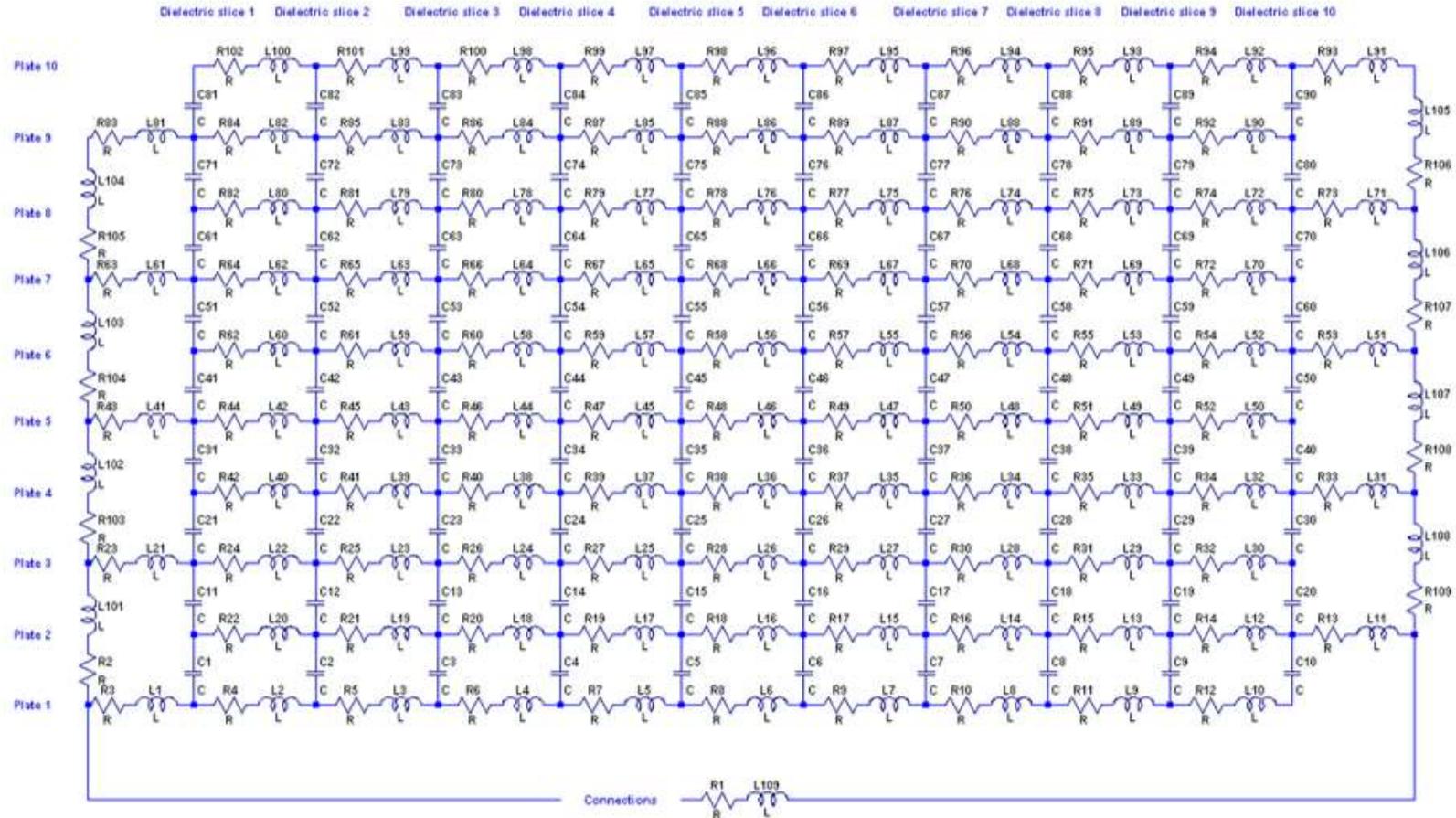
# ESR and DC Bias in Class II MLCC

- ESR does not change above SRF
- ESR increases below SRF as C drops
- Piezo effect shows up with increasing bias



# Secondary Effects: 2D Models

## Two-dimensional bedspring model

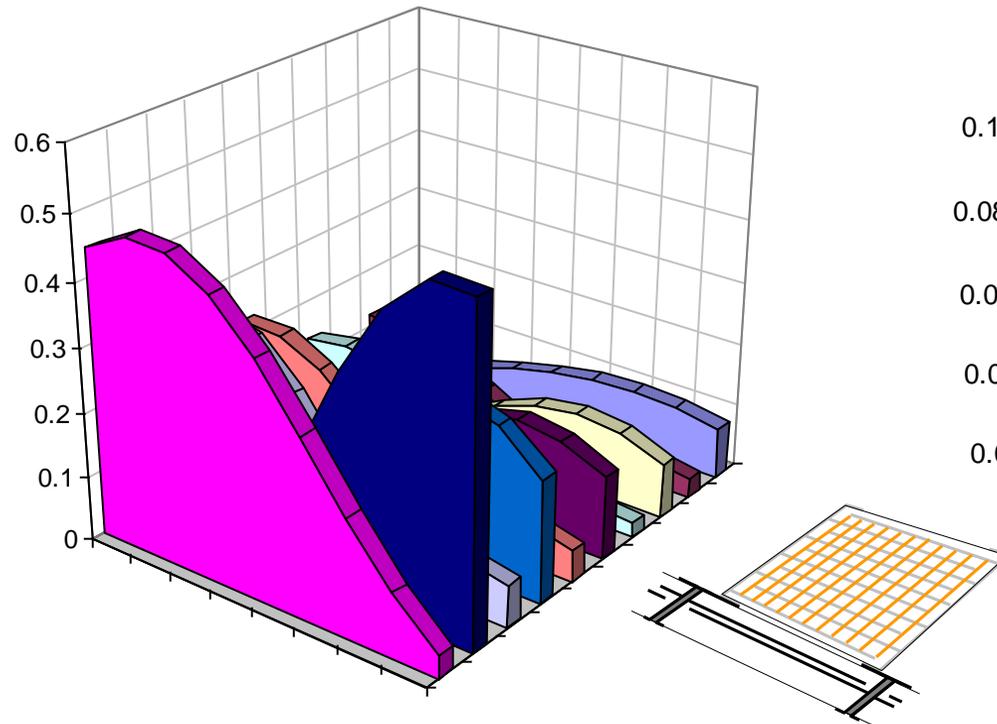


# Secondary Effects: 2D Models

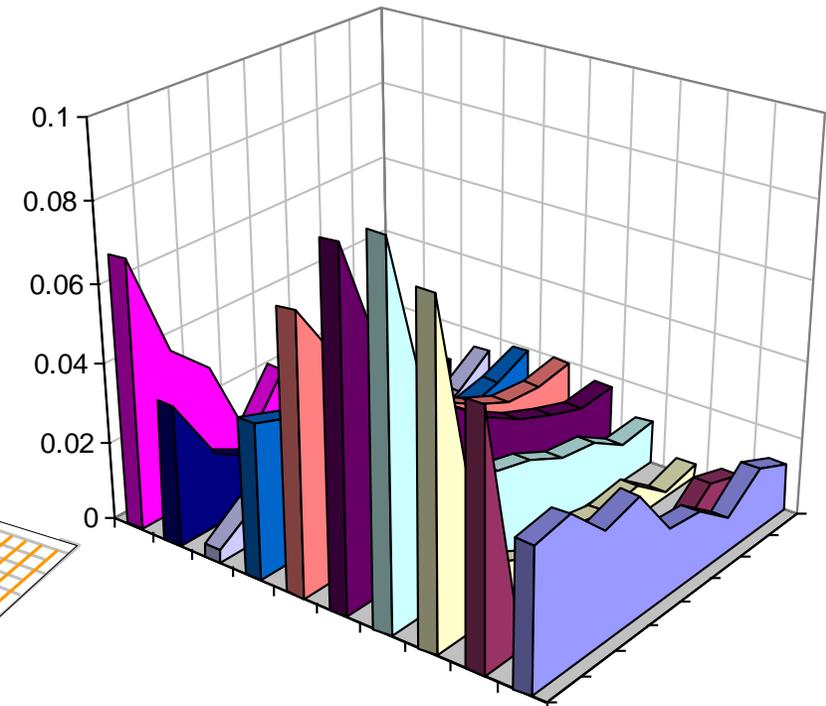
Internal current flow of MLCC at high frequencies captured with the 2D bedspring model.

Note: the horizontal and vertical resonances

Plate current at high frequency [A]



Dielectric current at high frequency [A]



# Secondary Effects: 3D Models

Simulates the internal geometry of the capacitor together with its immediate vicinity  
 Produces S-parameter data

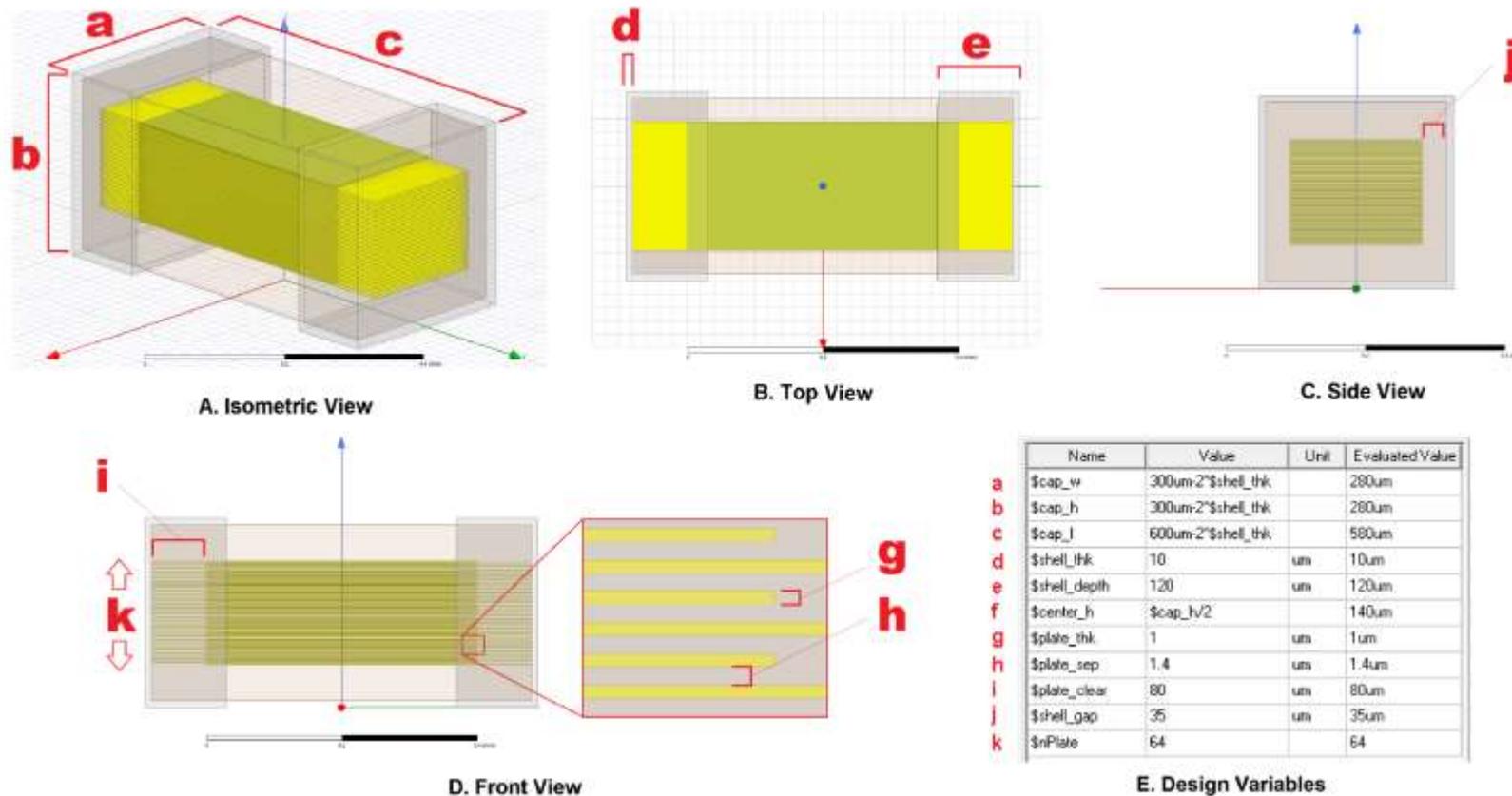


Figure 5 – HFSS 3D MLCC Model

# Summary and Conclusions

- Capacitor ESR represents the combined conductive and dielectric losses
- The frequency dependency is a complex function of material and geometry
- High-density ceramic capacitors can exhibit secondary resonances and piezo effect
- ESR variation drives up PDN worst-case transient noise
- Secondary effects can be simulated by 2D and 3D models



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[samtec.com/geekspeek](https://samtec.com/geekspeek)



[geekspeek@samtec.com](mailto:geekspeek@samtec.com)



[SIG@samtec.com](mailto:SIG@samtec.com)